

Rheology and Transport in Active and Passive Filaments

by
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Certificate

This is to certify that the thesis entitled “**Rheology and Transport in Active and Passive Filaments**” submitted by Sudipto Muhuri for the award of the degree of Doctor of Philosophy of Jawaharlal Nehru University is his original work. This has not been published or submitted to any other University for any other Degree or Diploma.

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Declaration

I hereby declare that the work reported in this thesis is entirely original. This thesis is composed independently by me at the Raman Research Institute under the supervision of Prof. Madan Rao. I further declare that the subject matter presented in this thesis has not previously formed the basis for the award of any degree, diploma, membership, associateship, fellowship or any other similar title of any university or institution.

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To write here, is like sleepwalking back, down the traversed lanes, recalling it all; the moments, people and the places - from the joyous dreams of the sparrow to the recurring sorrow. And while my thoughts are crisscrossing across this long span of time, touching every note of this experience that has been embedded in me like a song, I guess I will have to start somewhere. Like they say in fairytales - 'Once upon a time', half a decade and more ago, back in Pune were my friends- Ash, Anandamohan and Shiva. To them I owe this urge to embark upon this journey of doing my Ph.D. Apart from that, their company has always been refreshing. Ash in particular, I especially remember, for the all the drunken steps together and his critical analysis of the events and politics of our times, which helped in shaping and forming my own views.

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Contents

1	Introduction	1
1.1	Brief description of cellular filaments : DNA, actin and microtubules	4
1.2	‘Single-Particle’ description of filaments	5
1.2.1	Passive Filaments	5
1.2.2	Active Filaments	6
1.3	Collective description of active filaments	8
1.4	Prelude to chapters	11
1.4.1	Chapter 2 : Sequence-dependent DNA elasticity - Implications for DNA-protein binding	11
1.4.2	Chapter 3 : Active oriented filaments — shear stabilization and rheology	11
1.4.3	Chapter 4 : Active bidirectional transport of vesicles on microtubules	12
1.4.4	Chapter 5 : Collective transport of interacting vesicles on microtubules	14
1.5	Conclusions	14
	Bibliography	15
2	Sequence - dependent elasticity of DNA : Implications for DNA-protein binding	19
2.1	Introduction	20
2.2	Elastic description of DNA	22
2.3	Sequence - distribution in a worm-like chain (WLC) model	23
2.3.1	Distribution of global elastic variables	24
2.3.2	Distribution of local elastic variables	37
2.4	Implications for DNA-protein binding	39
2.5	Conclusions	45
	Bibliography	47

3	Active oriented filaments: shear stabilization and rheology	51
3.1	Introduction	52
3.2	Modeling active stress	53
3.3	Review of active hydrodynamics and rheology in the isotropic phase	55
3.3.1	Hydrodynamic equations in the isotropic phase	55
3.3.2	Linear rheology of a suspension of isotropic active filaments	57
3.4	Active hydrodynamics of the orientationally ordered phase in a shear flow	58
3.4.1	Hydrodynamic equations in the oriented phase with shear	58
3.4.2	Homogeneous steady state	60
3.4.3	Dynamics of fluctuations	61
3.4.4	Fluctuation spectrum	63
3.4.5	Instability in the absence of external shear	63
3.4.6	Non-equilibrium stability diagram in $d = 2$	64
3.4.7	Shear flow induced stabilisation in $d = 3$	65
3.5	Rheology in the oriented phase	66
3.6	Conclusions	67
	Bibliography	68
4	Active bidirectional transport of vesicles on microtubules	71
4.1	Introduction	72
4.2	Bidirectional transport	73
4.3	Single-particle model for bidirectional transport with multiple processive motors	76
4.3.1	The model	77
4.3.2	Steady state	78
4.3.3	Modeling velocity and (un)binding rates	80
4.4	Results	82
4.4.1	Steady state distribution of vesicles	82
4.4.2	Average number of bound motors	82
4.4.3	Velocity distribution	83
4.4.4	Mean first passage time	86
4.4.5	Reversal time of vesicles	87
4.5	Conclusions	90

Bibliography	91
5 Collective transport of interacting vesicles on microtubules	93
5.1 Introduction	94
5.2 A minimal model for bidirectional transport: 4-species model	95
5.2.1 Dynamic rules	96
5.2.2 Equations of motion	97
5.3 Steady state for ‘fast’ inter-conversion rates	99
5.4 Mean-field and continuum limit	99
5.4.1 Equations of motion in bulk	100
5.4.2 Steady state	101
5.4.3 Matching conditions at the boundaries	101
5.5 Phase diagram and domain wall analysis	102
5.5.1 The phases	102
5.5.2 Selection of phases: domain wall dynamics	103
5.5.3 Domain wall boundaries	107
5.6 Conclusions	110
Bibliography	111