

ELECTRIC AND MAGNETIC FIELD EFFECTS IN LIQUID CRYSTALS

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DECLARATION

I hereby declare that the thesis
was composed by me independently and
that it has not formed the basis for the
award of any Degree, Diploma, Associate-
ship, Fellowship or other similar title.



PRAKASH P. KARAT

'CERTIFIED'



CERTIFICATE

I certify that this thesis has been composed by Mr. Prakash P. Karat based on investigations carried out by him at the Liquid Crystals Laboratory, Raman Research Institute under my supervision. The subject matter of this thesis has *not* previously formed the basis of the award of any degree, diploma, associateship, fellowship or other similar title.



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PREFACE

This thesis describes some investigations on the effects of magnetic and electric fields on nematic liquid crystals. These investigations may be classified broadly into four parts:

- (a) New methods of optical detection of field induced deformations (Chapters II and VI) ;
- (b) Study of the elastic constants in relation to long range orientational order (Chapters III and IV) ;
- (c) Study of the elastic constants in relation to short range order (Chapter V) ;
- (d) Static and dynamic effects of electric fields (Chapters VII and VIII) .

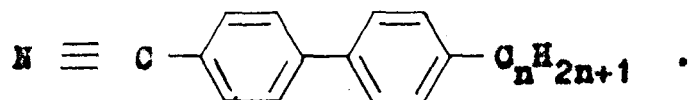
In Chapter I we give a general introduction to the subject with particular reference to the investigations reported in the rest of the thesis.

In Chapter II, we present a new method of determining the twist elastic constant (k_{22}) of nematic liquid crystals. In the usual configuration in which the nematic is homogeneously aligned

between two glass plates with the director anchored to the walls at either end, a small twist deformation in the medium cannot be detected optically when light is incident normal to the sample plane because the electric vector merely follows the director (Mauguin 1911). This is a consequence of the large birefringence of the medium for this direction of propagation, so that the phase retardation per unit length is very large compared to the twist per unit length. Under such circumstances, the 'adiabatic theorem' holds good. It is shown that the transition from the undistorted to the distorted state can be observed optically if the birefringence is small. To reduce the effective birefringence an experimental set up is described in which light is allowed to enter the sample obliquely, i.e., making a very small angle with respect to the sample plane (instead of being normal to it). The temperature variations of k_{22} of p-azoxyanisole (PAA) and p-azoxyphenetole (PAP) measured by this method are presented. Independent measurements on different samples give consistent results and moreover the data on PAA agree well with those reported earlier, confirming that this simple method is a reliable one. The temperature variation of k_{22} of PAA and PAP shows an S^2 dependence (S being the order parameter) in

conformity with the mean field theory. This new method was used in all the measurements of k_{22} which are described in subsequent chapters.

In Chapter III we present experimental determinations of the splay (k_{11}), twist (k_{22}) and bend (k_{33}) elastic constants and the order parameter (S) as functions of temperature for the 5th, 6th, 7th and 8th homologues of 4'-n-alkyl-4-cyanobiphenyls (nCB)



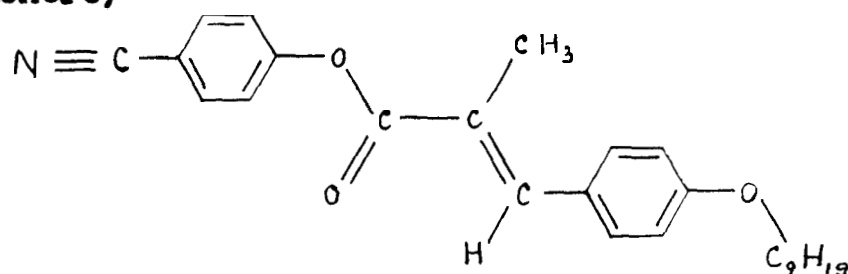
5CB, 6CB and 7CB show only the nematic phase, while 8CB shows the smectic A phase as well at lower temperatures. These compounds are strongly polar, room temperature liquid crystals with large positive dielectric anisotropy. X-ray diffraction studies (Leadbetter et al. 1975) show that these compounds belong to the class of normal cybotactic nematics wherein small groups with smectic-like order are present even in the isotropic phase. Furthermore, the compounds form double layers with interdigitated molecules, because of the antiparallel correlation between the strongly polar nitrile groups attached to one end of the molecule. The results obtained

by us show some interesting features. In the first place k_{33} and to some extent k_{11} deviate from the S^2 dependence. They increase more rapidly as the temperature is decreased. On the other hand k_{22} shows the S^2 dependence (except in the case of 8CB, which will be discussed in the fifth chapter). These results can be interpreted to mean that the temperature variations of the longitudinal and transverse correlation lengths ($\xi_{||}$ and ξ_{\perp}) are unequal. However the ratios of the elastic constants in 5CB, 6CB and 7CB are practically the same (at any given relative temperature $(T_{NI} - T)$). This suggests that the temperature variation of short range order is similar in these compounds, although the absolute values of the short range order are not the same.

Near T_{NI} , k_{33} shows the odd-even effect whereas S shows alternation only for the first three members studied and increases from 7CB to 8CB. The latent heat of transition (ΔH), k_{11} and k_{22} show the same trend as S . ~~(figure 1)~~ Moreover near T_{NI} , k_{33} is less than k_{11} for 8CB which is a most unusual result. These observations can be interpreted by assuming that the ratio ($\xi_{||}/\xi_{\perp}$) near T_{NI} decreases between 7CB and 8CB.

Measurements of k_{11} and S have also been made

on another series of new compounds prepared recently in our chemistry laboratory (Sadashiva 1976), viz., **trans-p-n-alkoxy- α -methyl cyanophenyl cinnamates (nOMCPC)**



These esters are colourless, chemically stable and possess high viscosity in the nematic phase. They also have a nitrile group attached to one end of the molecule and exhibit strong positive dielectric anisotropy. We have studied the second, third, fourth and eighth, ninth and tenth homologues of this series. (The other members were not investigated because they have a short nematic range, and, furthermore, most of them are monotropic). Of these 10 OMCPC shows a monotropic smectic A phase. The results on this series, discussed in Chapter IV, are more complicated than in the case of cyanobiphenyls. For instance, S and ΔH increase considerably between 4 OMCPC and 8 OMCPC. k_{33} and to a smaller extent k_{11} also exhibit an upward jump between these two members. However T_{NI} and k_{22} do not show any such jump. Moreover the

ratios of elastic constants at the same relative temperature differ considerably among the different compounds studied. Both k_{11} and k_{22} broadly follow an S^2 dependence in the second, third, fourth and eighth homologues with the exception of k_{22} of 4 OMCPG which exhibits a significantly slower variation. On the other hand k_{33} varies more rapidly with temperature in all cases.

As yet, no X-ray data are available on the compounds. Since the molecules are strongly polar, it is probable that they form double molecular layers, as in the case of other polar molecules (McMillan 1973, Leadbetter et al. 1975). It is observed that the melting point of the crystal decreases steadily between second and fourth members in the series, and shows a large increase between the fourth and fifth homologues. Thereafter it again decreases steadily till the ninth member. It is possible that the crystal structure changes between fourth and fifth members and the nature of short range order may also be different between the lower (≤ 4) and higher (≥ 5) homologues. This may explain the trends in the physical properties that are described above.

In Chapter V we describe some studies on the critical divergence of k_{22} and k_{33} near the A-N transition.

In particular we have made measurements on 8CB, 10 OMCP, p-cyanobenzylidene-p-n-octyloxyaniline (CBOOA) and octyloxy cyanobiphenyl (8 OCB). To increase the nematic range we prepared two mixtures of 8 OCB and 7CB. de Gennes has shown that in these cases the twist and bend constants can be expressed as $k_{11} = (k_{11})_0 + C_2(T - T^*)^{-\gamma}$ when $(k_{11})_0$ is the 'normal' elastic constant (in the absence of correlations). $T^* = T_{AN}$ if the transition is strictly second order. In all the compounds studied except 8CB, the values of γ is around 0.6. For 8CB in which the A-N is distinctly first order $\gamma \sim 1.0$. However it must be emphasized that a quantitatively meaningful estimate of the critical exponent requires the measurement to be carried out within a few millidegrees of the transition. In the present study the measurements were not made to this degree of precision and the value of γ obtained here cannot be regarded as accurate enough to throw any light on the question of whether the A-S transition exhibits helium like or classical mean field behaviour. (Indeed this objection is probably valid in many of the previous studies, e.g., Cheung *et al.* 1973, Delaye *et al.* 1973).

In Chapter VI we present measurements of the threshold for a twisted nematic cell (TN cell). The

TN cell has gained importance in recent years because of its use in display devices. The theory of the TN cell was developed by Leslie (1970), who derived an expression for the threshold magnetic field (H_L) beyond which deformation occurs in the sample. It is well known that when viewed through parallel polarizers kept parallel or perpendicular to the director at either bounding surface, the optical threshold (H_0) is always greater than H_L (Gerritsma et al. 1971). This is again due to the adiabatic theorem referred to earlier. We show that H_L can be determined optically, if the set up is sensitive to 8—11 changes in the birefringence of the sample. Using this method, we have determined the threshold H_L accurately. Using k_{11} , k_{22} and k_{33} values (from Chapter III), we have checked that Leslie's expression for the critical field agrees well with the observed value. Further, we have shown that $H_L x_0$ (x_0 being the sample thickness) is independent of sample thickness proving that H_L is the true Leslie threshold. This is the first verification of Leslie's theory for the twisted nematic cell.

The next two chapters discuss some electric field effects. It is well known that nematic liquid crystals have a low frequency dielectric relaxation (\sim MHz) which is due to the reorientation of the

dipoles about an axis normal to the director. This relaxation can be understood in terms of the nematic potential, which a molecule has to overcome in trying to rotate about its short axis (Meier and Saupe 1966).

In Chapter VII we present a study of this low frequency relaxation by observation of the Fredericksz threshold both in the k_{33} and k_{11} geometries. The principle is to measure the critical magnetic field corresponding to the Fredericksz transition in the presence of an alternating stabilising electric field. The electric field is along the undistorted director axis and the magnetic field normal to it. As the frequency of the electric field approaches the frequency of relaxation the critical magnetic field (H_c) decreases considerably and tends to approach H_0 . In the case of 6CB, even for frequencies higher than the relaxation frequency, $H_c > H_0$ (the value in zero electric field), i.e., the dielectric anisotropy remains weakly positive. However in the case of 9 OMCP, beyond a particular frequency f_0 (depending upon the temperature) H_c becomes less than H_0 indicating that $\Delta \epsilon$ has changed sign. The graph of $\log f_R$ (relaxation frequency) vs. $\frac{1}{T}$ gives a slope which is proportional to the total activation energy Q . For 9 OMCP, Q was estimated to be 1 eV. We have also made observations of the Fredericksz

threshold in the k_{11} geometry due to an electric field (with no magnetic field present). In the case of 9 OMCP a critical field does not pertain to a pure Fredericks transition at very high frequencies (> 1 MHz) since electrohydrodynamic instability makes a strong contribution. Indeed as the electric field is increased beyond the threshold value striations analogous to 'Williams domains' are seen. The domain width has the same order of magnitude as the sample thickness. Possible mechanisms for this high frequency instability are discussed briefly.

In Chapter VIII we present some new types of optical patterns due to electrohydrodynamic instabilities in nematic MBBA. The usual method of observing these domains is to use the 'sandwich' geometry, the direction of observation being along the electric field. We have used a geometry in which the direction of observation is along the initial undistorted director axis and normal to the applied electric field. Just above the threshold voltage, it appears that the vortices are in the plane containing the electric field and the direction of observation. With increase of the voltage the patterns observed become complicated and three dimensional flow patterns are seen. The domain widths are approximately half the electrode

separation. However the threshold voltage is much larger than that in the usual sandwich geometry. An explanation is given of the origin of this type of flow pattern.

Another interesting observation presented in this Chapter is the effect of electric fields on nematic droplets of MBBA suspended in its isotropic phase. The drops which appear spherical at zero field, become ellipsoidal with its major axis normal to the field. For very high fields the droplets acquire highly distorted, rapidly changing shapes. These deformations are observed both in DC and low frequency AC fields. As the frequency is increased, the deformation decreases and for high frequency ~ 5 KHz no deformation is seen. The origin of this type of distortion is again electrohydrodynamic, but a detailed theory of the observed behaviour still remains to be developed.

Some of the results discussed in this thesis are reported in the following publications:

1. Some electrohydrodynamic distortion patterns in a nematic liquid crystal (N.V. Madhusudana, P.F. Karat and S. Chandrasekhar) - Current Science 42(5), 147-149 (1973).

2. Experimental determination of the twist elastic constant of nematic Liquid crystals (N.V. Madhusudana, P.P. Karat and S. Chandrasekhar) - Presented at the International Liquid Crystals Conference, Bangalore December 1973 - Pramana Suppl. 1, 225-236 (1975).
3. Some new types of electrohydrodynamic flow patterns in nematic liquid Crystals (P.P. Karat, N.V. Madhusudana) - Presented at the International Liquid Crystals Conference, Bangalore, December 1973 - Pramana Suppl. 1, 285-288 (1975).
4. Elastic and optical properties of some 4'-n-alkyl-4-cyanobiphenyls (P.P. Karat and N.V. Madhusudana) - Molecular Crystals & Liquid Crystals 36, 51 (1976).
5. Elasticity and orientational order in some 4'-a-alkyl-4-cyanobiphenyls: Part II (P.P. Karat and N.V. Madhusudana) - Mol. Cryst. Liquid Cryst. (In press).
6. Verification of Leslie's expression for the threshold field for a twisted nematic cell (P.P. Karat and N.V. Madhusudana) - Mol. Cryst. Liquid Cryst. (in press).
7. A study of the dielectric relaxation in nematic liquid crystals using the Freedericksz transition technique (P.P. Karat and N.V. Madhusudana) - Mol. Cryst. Liquid Cryst. (in press).

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